

The Backflow Algorithm

Lecture 37
Section 8.5

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- 1 Critical Paths
- 2 The Backflow Algorithm
- 3 Practice
- 4 Assignment

Outline

- 1 Critical Paths
- 2 The Backflow Algorithm
- 3 Practice
- 4 Assignment

Definitions

Definition (Critical Path for a Vertex)

The **critical path for a vertex** is the path of longest processing time from that vertex to END.

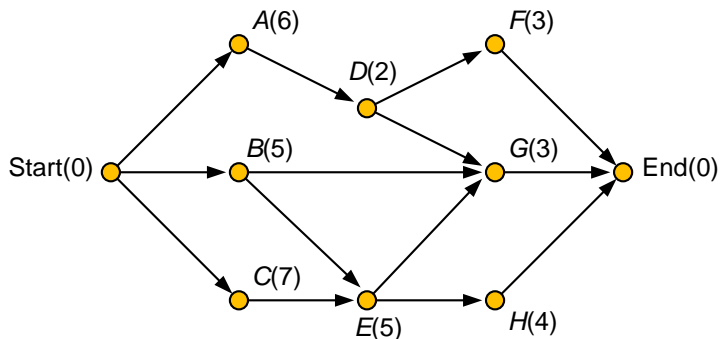
Definition (Critical Path for a Project)

The **critical path for a project** is the critical path from START to END.

Definition (Critical Time)

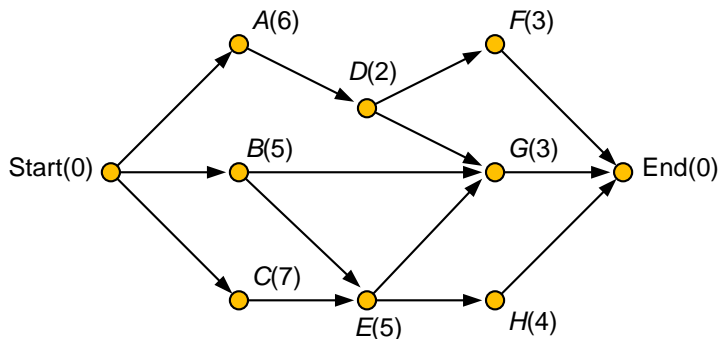
The **critical time** for a vertex or project is the processing time of its critical path.

Example



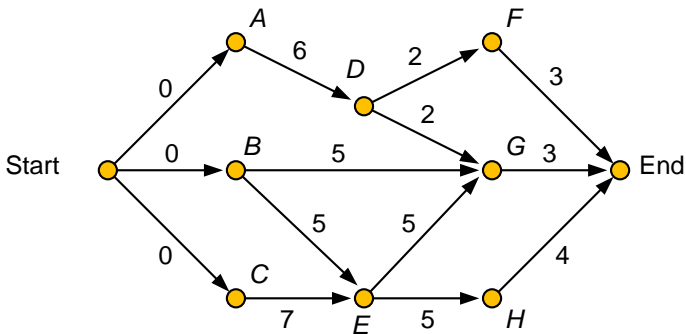
- The critical time of a project is the **shortest** possible time required to complete the project.

Example



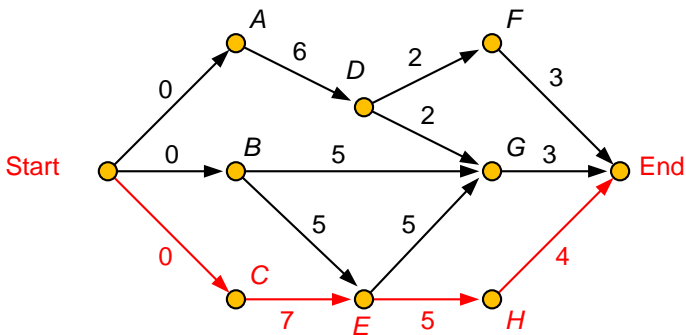
- The critical time of a project is the **shortest** possible time required to complete the project.
- It is also the **longest** path (in terms of time) from START to END.

Example



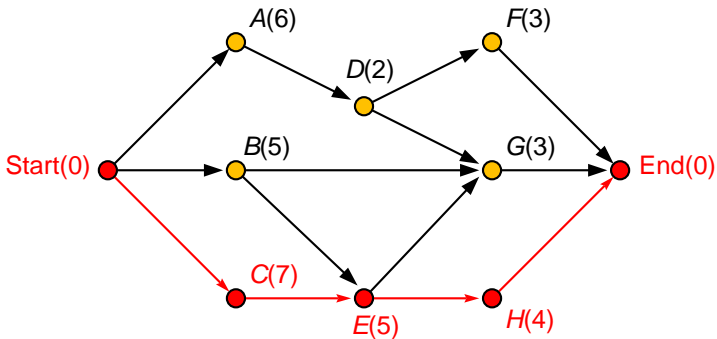
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Example



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The Backflow Algorithm

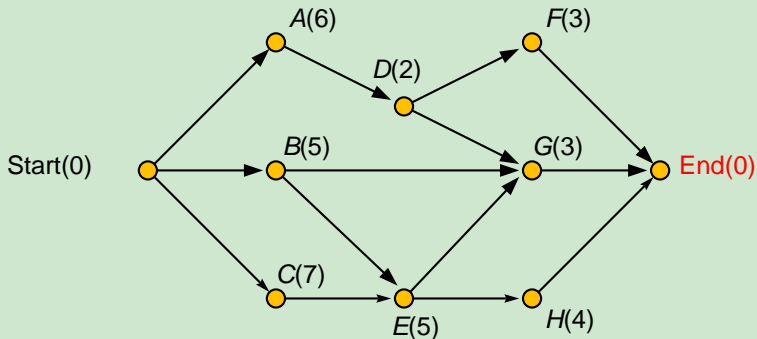
Definition (The Backflow Algorithm)

The **backflow algorithm** finds the critical path by the following method.

- 1 Beginning with END and working back to START, find the critical time for each vertex.
 - The critical time for a vertex is the processing time for that vertex plus the largest critical time of its immediate successors.
- 2 The critical path for the project is the path from START to END whose edges connect each vertex to its successor with the greatest critical time.

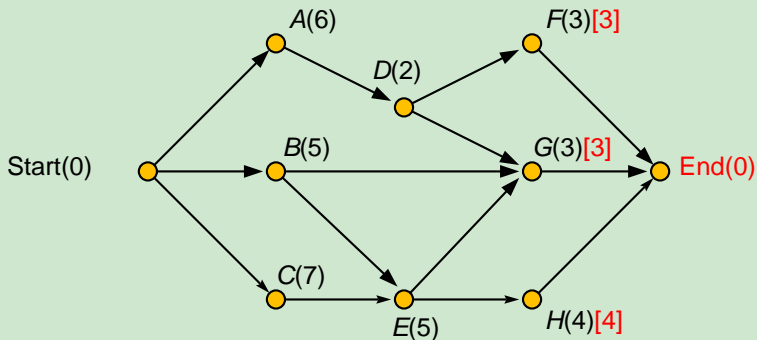
The Backflow Algorithm

Example (The Backflow Algorithm)



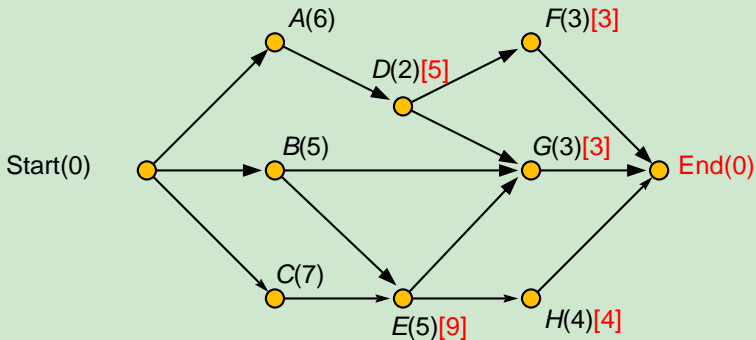
The Backflow Algorithm

Example (The Backflow Algorithm)



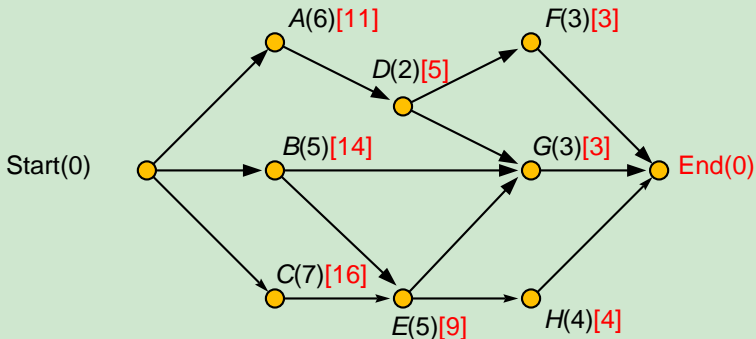
The Backflow Algorithm

Example (The Backflow Algorithm)



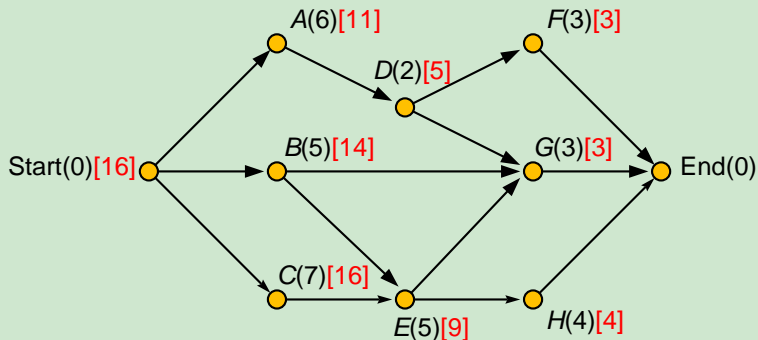
The Backflow Algorithm

Example (The Backflow Algorithm)



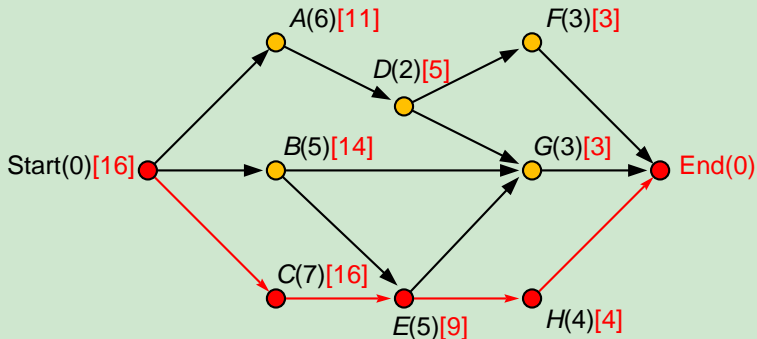
The Backflow Algorithm

Example (The Backflow Algorithm)



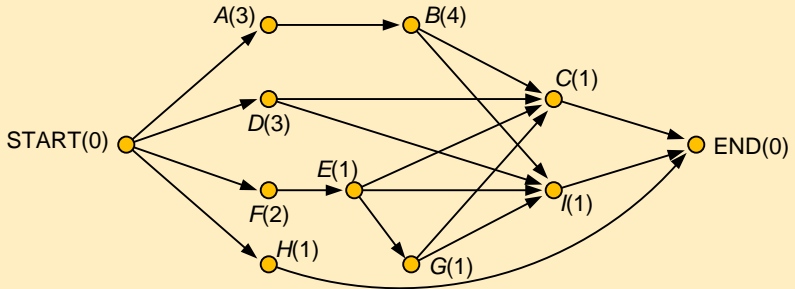
The Backflow Algorithm

Example (The Backflow Algorithm)



Example

Planning a Meeting



Outline

1 Critical Paths

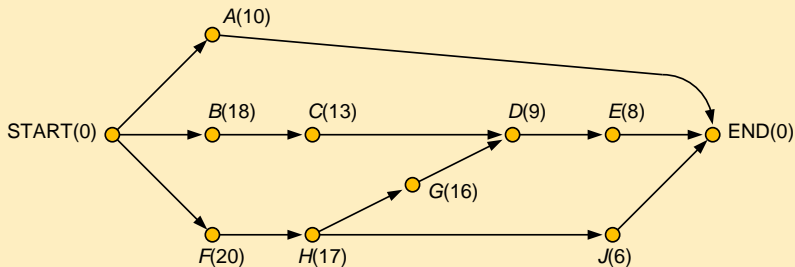
2 The Backflow Algorithm

3 Practice

4 Assignment

Practice

Practice



- Use the Backflow Algorithm to find the critical path.

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- 1 Critical Paths
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Assignment

Assignment

- Chapter 8: Exercises 49, 50, 51, 52, 56.